## UNIVERSITY COLLEGE OF ENGINEERING KAKINADA (AUTONOMOUS) DEPARTMENT OF ELECTRONICS & COMMUNICATION ENGINEERING

Name of the Course: Random Variables & Stochastic Processes Class: II B.Tech I-Sem Academic Year: 2019-20

## Tutorial # 2

- 1. Write the expression for the mean value of a discrete random variable.
- 2. Write the expression for the mean value of a continuous random variable.
- 3. Define the  $n^{th}$  moment of a random variable.
- 4. Define  $n^{th}$  central moment of a random variable.
- 5. A random variable X has a probability density function of the form

 $f_X(x) = \exp(-2|x|) - \infty < x < \infty$ . A second random variable Y is related X by

 $Y = X^2$ . Find the probability density function of the random variable *Y*. Find the probability that *Y* is greater than 2.

- 6. When three coins are tossed, the random variable is taken to be the number of heads that result. Find
  - a) the mean value of this random variable
  - b) the variance of this random variable
- 7. A Gaussian random voltage has a mean value of 5 and variance of 16.
  - a) What is the probability that an observed value of the voltage is greater than zero?
  - b) What is the probability that an observed value of the voltage is greater than twice the mean value?
- 8. A current having a Rayleigh probability density function is passed through a resistor having a resistance of  $2\pi \Omega$ . The mean value of the current is 2 A.
  - a) Find the mean value of the power dissipated in the resistor.
  - b) Find the probability that the dissipated power is greater than 72 W.
- 9. Define the characteristic function (CF) of a random variable and show that the moments can be obtained from CF.
- 10. Define the moment generating function (MGF) of a random variable and show that the moments can be obtained from MGF.